Market Models

A Guide to
Financial Data Analysis

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Chichester • New York • Weinheim • Brisbane • Singapore • Toronto

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Pure Monopoly models are where a single product or maker controls the market. There are no competitors, and the provider can theoretically drive up prices as they like. Examples of pure monopolies include entities like utility companies and government-run liquor stores. The market model says that the return on a security depends on the return on the market portfolio and the extent of the security's responsiveness as measured by beta. The return also depends on conditions that are unique to the firm. The market model can be graphed as a line fitted to a plot of asset returns against returns on the market portfolio. This relationship is sometimes called the single-index model. Most Popular Terms: Earnings per share (EPS). Hiring English speaking models. The topic is Financial Analysis. To apply send photo and contact information toÂ See more of Market Models on Facebook. Log In. or. Create New Account. See more of Market Models on Facebook. Log In. Forgotten account?